# Electronic and vibrational properties of  $\gamma$ -AlH<sub>3</sub>

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Aluminum hydride (alane) AlH<sub>3</sub> is an important material in hydrogen storage applications. It is known that AlH<sub>3</sub> exists in multiply forms of polymorphs, where  $\alpha$ -AlH<sub>3</sub> is found to be the most stable with a hexagonal structure. Recent experimental studies on  $\gamma$ -AlH<sub>3</sub> reported an orthorhombic structure with a unique doublebridge bond between certain Al and H atoms. This was not found in  $\alpha$ -AlH<sub>3</sub> or other polymorphs. Using density functional theory, we have investigated the energetics, and the structural, electronic, and phonon vibrational properties for the newly reported  $\gamma$ -AlH<sub>3</sub> structure. The current calculation concludes that  $\gamma$ -AlH<sub>3</sub> is less stable than  $\alpha$ -AlH<sub>3</sub> by 1.2 KJ/mol, with the zero-point energy included. Interesting binding features associated with the unique geometry of  $\gamma$ -AlH<sub>3</sub> are discussed from the calculated electronic properties and phonon vibrational modes. The binding of H-*s* with higher energy Al-*p*,*d* orbitals is enhanced within the double-bridge arrangement, giving rise to a higher electronic energy for the system. Distinguishable new features in the vibrational spectrum of  $\gamma$ -AlH<sub>3</sub> were attributed to the double-bridge and hexagonal-ring structures.

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#### **I. INTRODUCTION**

Aluminum hydride  $\text{AlH}_3$  (alane) is among the most promising metal hydrides for the hydrogen storage medium, containing a usable hydrogen fraction of 10.1 wt. % with a density of 1.48 g/ml. The enthalpy of the reaction is found to be low, resulting in minimal heat exchange for both charging and discharging reactions. This material is thermodynamically unstable near ambient conditions, but it is kinetically stable without releasing much hydrogen for years. However, extremely high hydrogen pressure (exceeding 25 kbar) is required to achieve charging. The decomposition of  $\text{AlH}_3$  occurs in a single step

$$
AIH_3 \to Al + \frac{3}{2}H_2.
$$
 (1)

<span id="page-0-0"></span>How to overcome the kinetic barriers and to find new routes to synthesize  $\text{AlH}_3$  for reversibility have been the focus of many research activities recently.

Early studies identified seven polymorphs of AlH<sub>3</sub>:  $\alpha$ ,  $\alpha'$ ,  $\beta$ ,  $\delta$ ,  $\varepsilon$ ,  $\gamma$ , and  $\xi$ .<sup>[1](#page-6-0)</sup> It was suggested experimentally that the  $\alpha$ phase is the most stable, followed by the  $\beta$  and  $\gamma$  phases.<sup>2[,3](#page-6-2)</sup> The decomposition of the  $\gamma$  and  $\beta$  phases is faster than that of  $\alpha$  phase. A reaction enthalpy of 7.1 and 11.4 KJ/mol-H<sub>2</sub> for  $\gamma$  and  $\alpha$ , respectively, is reported.<sup>2[,3](#page-6-2)</sup> This translates to an enthalphy difference of 6.4 KJ/mol between the  $\alpha$  and  $\gamma$ phases. The exothermic transition to the  $\alpha$  phase from the  $\gamma$ phase is also reported. Only the  $\alpha$  polymorph AlH<sub>3</sub> has been experimentally investigated extensively, including structural characterization,<sup>4</sup> thermodynamic measurements,  $5,6$  $5,6$  and ther-mal and photolytic kinetic studies.<sup>6-[12](#page-7-0)</sup> Theoretical calculations<sup>13–[15](#page-7-2)</sup> of  $\alpha$ -AlH<sub>3</sub> from first principles have been performed to study the structural stability and electronic and thermodynamic properties. Limited studies have been conducted on other polymorphs and their properties.

Recently, the crystal structure of  $\gamma$ -AlH<sub>3</sub> is reported by two separate groups using synchrotron x-ray powder diffraction<sup>16</sup> and powder neutron diffraction,<sup>17</sup> respectively. A unique feature of double-bridge bonds involving Al-2H-Al is identified in addition to the normal bridge bond of Al-H-Al as found in  $\alpha$ -AlH<sub>3</sub>. In the present study, using density functional theory and the linear response approach, we investigate the electronic properties and phonon spectra for the newly published  $\gamma$ -AlH<sub>3</sub> crystal structure.<sup>16[,17](#page-7-3)</sup> The phase stability and interesting binding characteristics in  $\gamma$ -AlH<sub>3</sub> are presented and compared with that of  $\alpha$ -AlH<sub>3</sub>. The origin of the cohesive energy difference in these two phases is discussed. Distinct phonon vibrational modes arising from the double-bridge and hexagonal ring structures are identified.

#### **II. CALCULATIONAL PROCEDURES**

The calculations are based on density functional theory.<sup>18</sup> The Kohn-Sham equations are solved in a plane-wave basis using the Vienna *ab initial* simulation package (VASP).<sup>[19](#page-7-5)[,20](#page-7-6)</sup> For the exchange-correlation functional, the generalized gradient approximation (GGA) of Perdew and Wang  $(PW91)^{21}$  $(PW91)^{21}$  $(PW91)^{21}$ is employed. The electron-ion interaction is described by ultrasoft pseudopotentials (USPP). $^{22}$  $^{22}$  $^{22}$  The *k* space integrals are evaluated using the sampling generated by the Monkhorst-Pack procedure.<sup>23</sup> The calculation for both  $\alpha$ - and  $\gamma$ -AlH<sub>3</sub> structures are performed with a *k*-point mesh of  $7 \times 7 \times 7$ . The relaxations of cell geometry and atomic positions are carried out using a conjugate gradient algorithm until the Hellman-Feynman force on each of the unconstrained atoms is less than  $0.01 \text{ eV/A}$ . The nuclear coordinates are first allowed to relax while the cell volume is fixed at the experimental value. Then simultaneous relaxations of the cell volume, shape and atom coordinates are conducted. For the total energy calculations, the plane-wave energy cutoff is 600 eV. The self-consistent total energy converges to within  $10^{-5}$ eV/cell.

The vibrational properties are studied with density functional perturbation theory within the linear response. $^{24}$  The PWSCF numerical code<sup>25</sup> was used in our calculations for the zero-point energies and phonon density of states. The primi-

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FIG. 1. (Color online) Crystal structures of (a) orthorhombic  $\gamma$ -AlH<sub>3</sub>, (b) hexagonal-ring structure in  $\gamma$ -AlH<sub>3</sub>, and (c) hexagonal  $\alpha$ -AlH<sub>3</sub>. The large and small spheres denote Al and H atoms, respectively.

tive cell of  $\alpha$ -AlH<sub>3</sub> has 8 atoms and that of  $\gamma$ -AlH<sub>3</sub> has 24 atoms. Their optimized equilibrium structures from the total energy calculations using VASP are indistinguishable with those using PWSCF. The dynamical matrices are obtained for a uniform grid of *q* vectors of  $4 \times 4 \times 4$  and  $3 \times 3 \times 3$  over the Brillouin zone of  $\alpha$ - and  $\gamma$ -AlH<sub>3</sub>, respectively. The dynamical matrix is then Fourier-transformed to real space and

<span id="page-1-1"></span>

FIG. 2. Difference charge density plots (see text) for in the planes containing Al and H atoms: (a)  $\gamma$ -AlH<sub>3</sub> (002) plane, (b)  $\gamma$ -AlH<sub>3</sub> (001) plane, and (c)  $\alpha$ -AlH<sub>3</sub> (010) plane. The solid squares and circles represent Al and H positions, respectively. The density contour interval is 0.001 electrons/ $(\AA^3)$ . Charge deficiency is represented by dashed lines, while the density increase near the hydrogen atoms is represented by solid lines.

the force-constant matrices are constructed, which are used to obtain the phonon frequencies at arbitrary points.

### **III. RESULTS AND DISCUSSIONS**

#### **A. Structure and energetics**

The structural characterization from an earlier highresolution synchrotron x-ray diffraction<sup>4</sup> study concluded that  $\alpha$ -AlH<sub>3</sub> has a rhombohedral lattice of space group  $\overline{R3c}$ (No. 167). Recent diffraction experiments<sup>16,[17](#page-7-3)</sup> determined that  $\gamma$ -AlH<sub>3</sub> has an orthorhombic unit cell with space group *Pnnm* (No. 58). The unit cell for  $\gamma$ -AlH<sub>3</sub> is shown in Fig.  $1(a)$  $1(a)$ , compared with the hexagonal  $\alpha$ -AlH<sub>3</sub> in Fig. 1(c). The experimentally reported lattice constants are listed in Table [I.](#page-2-0) The building element for both phases is the  $\text{AlH}_6$  octahedron, where one Al atom is surrounded by six H atoms. However, the packing scheme in  $\gamma$ -AlH<sub>3</sub> is more complex than that in  $\alpha$ -AlH<sub>3</sub>. The AlH<sub>6</sub> octahedra are connected simply by sharing vertices in  $\alpha$ -AlH<sub>3</sub>, as illustrated in Fig. [1](#page-1-0)(c). The network of these octahedra produces only one type of Al-H-Al bridge bond which has a bond angle and a bond length of 142 $\degree$  and 1.712 Å, respectively. In contrast, in  $\gamma$ -AlH3 the  $\text{AlH}_6$  octahedra are connected not only by sharing vertices as



<span id="page-2-0"></span>TABLE I. Calculated cohesive energies (without the zero-point energy, but with the spin-polarization energy, see text) and structural parameters for  $\gamma$ -AlH<sub>3</sub> and  $\alpha$ -AlH<sub>3</sub> compared with values from experiments and previous calculations.

in  $\alpha$ -AlH<sub>3</sub>, but also by sharing edges, as shown in Fig. [1](#page-1-0)(a). As a consequence, two nonequivalent Al atoms, Al1 and Al2, are created. Four nonequivalent H atoms (H1-H4) (Ref. [16](#page-6-5)) are also identified as shown in Fig.  $1(a)$  $1(a)$ , while only one type H atom exists in  $\alpha$ -AlH<sub>3</sub>. Al1 is involved with the normal bridge bond with H, which is similar to that in  $\alpha$ -AlH<sub>3</sub> but with a slight difference in the bond length and angle. However, Al2 involves a new type of double-bridge configuration Al2-2H3-Al2, as shown near the center of unit cell in Fig.  $1(a)$  $1(a)$ . This double-bridge arrangement gives a smaller distance of 2.60 Å between the two Al2 atom compared with the Al-Al separation of 3.24 Å in  $\alpha$ -AlH<sub>3</sub> and 2.86 Å in Al metal. In addition to the new double-bridge configuration, a hexagonal-ring structure is found consisting of two Al2, two Al[1](#page-1-0), and four H4 atoms, as shown in Fig.  $1(b)$ . The four Al atoms are on one plane parallel to the *c* axis while the H4 atoms have a slight displacement  $(\sim 0.14 \text{ Å})$  out of this plane. These rings are connected to form linear chains along the *c* axis. The structures of the double bridge in the *ab* plane and the hexagonal-ring along the *c* axis are unique to  $\gamma$ -AlH<sub>3</sub> and have not been found in any other hydrogen-containing aluminum compounds. Furthermore, the  $\alpha$  phase possesses a higher order of symmetry than that of the  $\gamma$  phase, with a smaller primitive trigonal unit cell. The total number of formula units (f.u.) in a unit cell is 2 and 6 for the  $\alpha$  and  $\gamma$ phases, respectively. The molecular volume (the density) for the  $\gamma$  phase is found to be higher (lower) than that of the  $\alpha$ phase by 11% (10%).

Using the experimentally established space groups and unit cells as shown in Fig. [1,](#page-1-0) the total energies and structural parameters for both the  $\alpha$  and  $\gamma$  phases are studied from first-principles calculations. The calculated results for the fully relaxed structures are summarized in Table [I.](#page-2-0) The theoretical lattice parameters are in good agreement with the observed values for both  $\gamma$ - and  $\alpha$ -AlH<sub>3</sub> and are consistent with the results from previous  $\alpha$ -AlH<sub>3</sub> calculations.<sup>13[,14](#page-7-12)</sup> The calculated cohesive energies indicate that  $\gamma$ -AlH<sub>3</sub> is energetically less stable than  $\alpha$ -AlH<sub>3</sub> by 2.3 KJ/mol, without considering the zero-point energy. The listed cohesive energies have included the atomic spin-polarization energies of 0.15 eV/atom for Al and 0.07 eV/atom for H. The calculated value is in fair agreement with the measured value of 6.4 KJ/mol.<sup>2[,3](#page-6-2)</sup> In addition, in  $\gamma$ -AlH<sub>3</sub> various bond lengths for nonequivalent Al and H atoms are evaluated and compared with recent experimental results of synchrotron x-ray powder diffraction<sup>16</sup> and powder neutron diffraction<sup>17</sup> in Table [II.](#page-2-1) Good agreements are found between the calculated and observed values. Without including the zero point en-ergy, the calculated reaction enthalpies for Eq. ([1](#page-0-0)) of  $\alpha$  and  $\gamma$ phases are  $9.2$  and  $10.8$  KJ/mol-H<sub>2</sub>, respectively, which are also consistent with the measured values. $2,3$  $2,3$ 

#### **B. Electronic structure**

The electronic structure of  $\gamma$ -AlH<sub>3</sub> is first analyzed by examining the charge distribution and charge transfer. The

<span id="page-2-1"></span>TABLE II. Interatomic distances ( $\AA$ ) and bond angles (deg.) obtained from the fully relaxed structure of  $\gamma$ -AlH<sub>3</sub>. The values from the synchrotron x-ray diffraction (Ref. [16](#page-6-5)) and the powder neutron diffraction (Ref. [17](#page-7-3)) are also included for comparisons.

Bond	Calc.	Refs. 16 and 17	Bond	Calc.	Refs. 16 and 17	Angle	Calc.	Refs. 16 and 17
$Al1-A12$	3.18	3.1679/3.155	$Al2-H1$	1.69	1.668/1.657	$AI1-H4-Al2$	134.7	124.0/133.88
$Al2-A12$	2.62	2.602/2.585	$Al2-H2$	1.70	1.664/1.678	$AI1-H2-A12$	168.8	171.0/169.99
$Al1-H2$	1.76	1.769/1.764	$Al2-H3$	1.72	1.70/1.755	$AI2-H1-Al2$	180.0	180.0/179.99
$Al1-H4$	1.72	1.784/1.696	$Al2-H4$	1.72	1.790/1.733	$AI2-H3-Al2$	97.3	100.7/97.53
			$H3-H3$	2.30	2.16/2.266	H4-A11-H4	85.9	76.34/85.00
						H4-A12-H4	176.3	170.63/176.84

<span id="page-3-0"></span>

FIG. 3. (Color online) Calculated electronic density of states (DOS) projected onto (a) H and (b) Al in  $\alpha$ -AlH<sub>3</sub>, as well as the total DOS for (c)  $\alpha$ -AlH<sub>3</sub> and (d)  $\gamma$ -AlH<sub>3</sub>. The Fermi level is at zero.

difference charge density  $\Delta \rho(\mathbf{r})$  is the difference between the total charge density of the solid and a superposition of the atomic charge with the same spatial coordinates as in the solid:

$$
\Delta \rho(\mathbf{r}) = \rho_{\text{solid}}(\mathbf{r}) - \sum_{i} \rho_{\text{atom}}^{i}(\mathbf{r} - \mathbf{R}_{i}),
$$
\n(2)

where the sum is over all the atoms. Figure [2](#page-1-1) shows such plots in the planes containing two different types of Al-H configurations in  $\gamma$ -AlH<sub>3</sub>. The solid squares and circles represent Al and H positions, respectively. The (002) plane shown in Fig.  $2(a)$  $2(a)$  contains one double-bridge bond Al2-2H3-Al2 and two other H atoms (H1 and H2), while the  $(001)$  plane shown in Fig.  $2(b)$  $2(b)$  contains a normal bridge H2-Al1-H2. The difference density plot shows the positive values (solid contours) at the H positions, indicating a charge transfer from Al to H. As a result, aluminum is positively and hydrogen is negatively charged. The maximum of contour lines is in the order of 0.014 electrons/ $(\hat{A})^3$  for both (a) and (b). The minimum is about  $-0.002$  electrons/ $(\AA)^3$  and the step size of the contours is 0.001 electrons/ $(\hat{A})^3$ . The zero difference charge density line forms a closed contour around H, leaving a negative charge density in the interstitial regions.

<span id="page-3-1"></span>

FIG. 4. (Color online) Calculated electronic density of states projected onto nonequivalent atoms in  $\gamma$ -AlH<sub>3</sub>. The Fermi energy is set to be zero.

In Fig.  $2(a)$  $2(a)$ , note that the positive contours of difference charge density are not exactly centered at the two H3 sites. The local maximum near each H3 is slightly shifted toward each other and the zero difference charge density line encloses both H3, showing some interactions between the H3 pair. In contrast, this is not seen for other H atoms, nor in the normal H-Al-H structure in  $\alpha$ -AlH<sub>3</sub>. The separation between the two H3 atoms in a double-bridge configuration is 2.3 Å, which is slightly smaller than that of other neighboring H pairs. The distance of the two Al2 atoms  $(2.62 \text{ Å})$  is also small compared with that in Al metal (2.86 Å). The contour lines in Fig.  $2(a)$  $2(a)$  also shows enhanced interactions between H-*s* and Al-*d* electrons. For comparison, the difference charge density for  $\alpha$ -AlH<sub>3</sub> is calculated and plotted in Fig.  $2(c)$  $2(c)$  for the (010) plane containing normal Al-H bonds. It is found that the normal bridge bond in  $\gamma$ -AlH<sub>3</sub> [Fig. [2](#page-1-1)(b)] has similar characteristics as that in  $\alpha$ -AlH<sub>3</sub> [Fig. [2](#page-1-1)(c)]. The binding between Al and H atoms involves a charge transfer in both  $\alpha$ - and  $\gamma$ -AlH<sub>3</sub>.

The total electronic densities of states (DOS) for both structures are calculated and plotted in Fig. [3.](#page-3-0) The projected DOS onto H and Al for  $\alpha$ -AlH<sub>3</sub> are also presented in Fig. [3.](#page-3-0) The angular-momentum projected DOS is evaluated by integrating over a sphere centered at each atom with a radius of 1.0 Å for Al and 0.9 Å for H, respectively. The choice of the H radius is based on the charge distribution around H in order to catch the charge transfer to H. The radius of Al is then chosen according to the Al-H bond length in order to

<span id="page-4-0"></span>

FIG. 5. (Color online) Total charge density for the lowest two energy bands projected onto the (002) plane, the same plane as shown in Fig.  $2(a)$  $2(a)$ . The solid circles and squares represent H and Al positions. The maximum, minimum, and interval of the contours are 0.134, 0.008, 0.0063 electrons/ $(\AA^3)$ , respectively. The length scale is shown in Å.

cover as much of the interstitial region as possible without overlapping the spheres. The Fermi energy is set to zero in these plots.

The current results for  $\alpha$ -AlH<sub>3</sub> are comparable with previous calculations[.13–](#page-7-1)[15](#page-7-2) The H-*s* component spans the whole energy range. The lowest peak from  $\sim$ -8.7 to -4.0 eV is found to correspond to H-*s* and Al-*s* states, while the higherenergy features are composed of H-*s* and Al-*p* or −*d* states. The total band width is similar in both  $\alpha$ - and  $\gamma$ -AlH<sub>3</sub>. A difference between the two is clearly seen near −7 eV, where a small gap is created in the low energy region in  $\gamma$ -AlH<sub>3</sub>. This new gap gives rise to a broad, separated DOS peak from −8.7 to − 7.0 eV.

In order to understand the new feature found in the DOS of  $\gamma$ -AlH<sub>3</sub>, the projected density of states onto nonequivalent Al and H atoms are analyzed in Fig. [4.](#page-3-1) The same radius values used in  $\alpha$ -AlH<sub>3</sub> are adopted for integrating over the spheres around Al and H atoms. The valence states below the Fermi energy can be grouped into three energy regions: the low  $(-8.7 - -7.0 \text{ eV})$ , the middle  $(-6.8 - -4.0 \text{ eV})$ , and the high  $(-4.0-0$  eV) energy regions.

The broad peak in the low-energy region of −8.7– −7.0 eV is composed of considerable H3-*s* and Al2-*s* states, with some *s* contributions from other H and Al atoms. This broad peak consists of the first two energy bands separated from the other bands by a small gap. In Fig. [5,](#page-4-0) the total charge density for these two bands is calculated and plotted for the  $(002)$  $(002)$  $(002)$  plane, the same plane shown in Fig.  $2(a)$ . The maximum, minimum and interval of the contours are 0.134, 0.008, and 0.0063 electrons/ $(\text{\AA})^3$ , respectively. It shows noticeable charge accumulation around the H3-H3 pair. In addition, in Fig. [6,](#page-4-1) the total charge density for the same lowest two bands is projected onto the plane of hexagonal-ring as defined in Fig.  $1(b)$  $1(b)$ . Charge is found around four H4 atoms as well as between two Al2 atoms. Therefore, the broad peak in the low energy region is attributed mainly to the unique

<span id="page-4-1"></span>

FIG. 6. (Color online) Total charge density for the lowest two energy bands projected onto the plane consisting of the hexagonalring structure as shown in Fig.  $2(b)$  $2(b)$ . The solid circles represent H4 atom positions. The maximum, minimum, and interval of the contours are 0.134, 0.008, and 0.0063 electrons/ $(\AA^3)$ , respectively. The charge distribution are around H atoms and between two Al2 atoms.

double-bridge and hexagonal-ring structures in  $\gamma$ -AlH<sub>3</sub>.

In fact, the projected DOS associated with H3 is reduced in the middle energy region  $(-6.8 - -4.0 \text{ eV})$  compared with other H atoms. The missing amplitude is shifted to both the low  $(-8.7 - -7.0$  eV) and high  $(-4.0 - 0$  eV) energy regions. The former contains an increased H3-H3 interaction and the H-*s* and Al2-*s* coupling, while the latter exhibits an enhanced interaction between H3-*s* and Al2-*p* and -*d* states. The stronger interaction of H3-*s* states with higher-energy Al2-*p* and -*d* states due to geometry gives rises to a higher electronic energy for the system.

## **C. Vibrational properties**

It is expected that the high vibrational frequencies of light hydrogen atoms may result in a significant zero-point energy, which needs to be included in studying the ground-state properties. In order to consider the zero-point energy  $E_{\text{zpt}}$ contributions to the energetics between the two AlH<sub>3</sub> phases,

<span id="page-4-2"></span>TABLE III. Phonon frequencies in cm−1 for optical normal modes at the  $\Gamma$  point calculated at experimental lattice constants for  $\alpha$ -AlH<sub>3</sub>. The previous LDA calculation from Ref. [13](#page-7-1) is included in parenthesis for comparison.

Mode Symmetry	Frequency $(cm-1)$
Infrared active:	
$E_u$	311(286), 632(583), 858 (851), 1750(1687)
$A_{2u}$	560(512), 1718(1650)
Raman active:	
$E_{g}$	497(490), 1034(993), 1520(1481)
$A_{1g}$	738(812)
Inactive:	
$A_{1u}$	370(345), 925(921)
$A_{2g}$	891(751), 1987(1903)

<span id="page-5-0"></span>

FIG. 7. (Color online) Total and partial phonon density of states (DOS) for  $\alpha$ -AlH<sub>3</sub>.

the phonon density of states (DOS) are evaluated for both  $\alpha$ and  $\gamma$ -AlH<sub>3</sub>. The obtained zero point energy for  $\alpha$ -AlH<sub>3</sub> is 167 meV/atom, which is good agreement with the previous results of 161 meV/atom (Ref. [13](#page-7-1)) and 165 meV/atom (Ref. [14](#page-7-12)). The calculated zero point energy for  $\gamma$ -AlH<sub>3</sub> is 164 meV/atom. Although the absolute value of  $E_{\text{znt}}$  is noticeable for the two phases, the difference turns out to be small  $\Delta E_{\text{zpt}} = E_{\text{zpt}}(\alpha) - E_{\text{zpt}}(\gamma) = 3$  meV/atom. By including this cor-rection to the total energies previously listed in Table [I,](#page-2-0) the  $\gamma$ phase has a slightly higher energy than the  $\alpha$  phase by 1.2 KJ/mol. At  $T = 300$  K, the calculated vibrational enthalpy  $H^{T=300 \text{ K}}$  (without zero point term) and entropy  $S^{T=300 \text{ K}}$  are 0.232 eV/f.u. and 3.75  $k_B$ /f.u. for  $\alpha$ -AlH<sub>3</sub>, 0.235 eV/f.u. and  $4.0 \frac{k_B}{f.u.}$  for  $\gamma$ -AlH<sub>3</sub>, respectively, where  $k_B$  is Bolzman constant. The small difference in the calculated quantities indicates the similarity of the thermodynamic properties between the two phases of alane.

The partial phonon density of states (DOS) for atom  $\tau$  is defined as

$$
\rho_{\tau}(\omega) = \sum_{q} \sum_{j=1}^{3N} |\mathbf{e}_{\tau}(\mathbf{q},j)|^2 \delta[\omega - \omega(\mathbf{q},j)], \tag{3}
$$

where  $N$  is the total number of atoms per unit cell,  $q$  is the phonon momentum, *j* labels the phonon branch,  $e_{\tau}(q, j)$  is the phonon polarization vector for atom  $\tau$ , and  $\omega(\mathbf{q}, j)$  is the phonon frequency. The total and projected phonon densities of states for  $\alpha$ - and  $\gamma$ -AlH<sub>3</sub> are presented in Figs. [7](#page-5-0) and [8,](#page-5-1) respectively. Our calculated phonon DOS for  $\alpha$ -AlH<sub>3</sub> is in good agreement with previous calculations,  $13,14$  $13,14$  showing three distinct groups in the whole frequency range. The decomposed phonon DOS indicates that the low frequency

<span id="page-5-1"></span>

FIG. 8. (Color online) Total and partial phonon density of states (DOS) for  $\gamma$ -AlH<sub>3</sub>.

modes below 350 cm−1 are mainly from Al atoms, while the middle and high frequency modes are H dominated. This is due to the large mass ratio between H and Al atoms. The high-frequency phonons above 1550 cm−1 are associated with H motion in the Al-H bond stretching modes. No vibrational modes was found in the frequency region from 1025 to 1550 cm<sup>-1</sup>, yielding a gap of 525 cm<sup>-1</sup> in  $\alpha$ -AlH<sub>3</sub>.

The phonon DOS for  $\gamma$ -AlH<sub>3</sub> is more complex than that for  $\alpha$ -AlH<sub>3</sub> due to the structural difference. The  $\gamma$ -phase unit cell has much more atoms (24) than the  $\alpha$  phase (8), therefore the calculated phonon DOS for  $\gamma$ -AlH<sub>3</sub> in Fig. [8](#page-5-1) exhibit more features. Comparing with the phonon DOS of  $\alpha$ -AlH<sub>3</sub>, although the modes located in the three frequency regions remain, multiple new additional peaks appear in the spectrum. In order to understand how different atomic species contribute to these vibrations, the partial phonon DOS is calculated for the four types of H and two types of Al atoms, as illustrated in Fig. [8.](#page-5-1)

The new features labeled in Fig. [8](#page-5-1) can be summarized as follows: (1) four new vibrational peaks appear within the gap region of the  $\alpha$ -AlH<sub>3</sub> spectrum in the frequency range of 1200 to 1500 cm−1. These are vibrational modes of H3 in the plane of the Al2-2H3-Al2 complex. It consists of both bond stretching and bending motions by H3 on this plane. (2) A new strong narrow peak is introduced in the middle frequency region around a frequency of 875 cm<sup>-1</sup>, corresponding to the H3 vibrations perpendicular to the Al2-2H3-Al2 plane. (3) An additional broaden peak appears in the lowfrequency region from 375 to 475 cm<sup>-1</sup>, which is dominated



<span id="page-6-6"></span>

by Al2 in-plane vibrational modes, coupled with some contributions from H1 and H2 atoms but with little contribution from H3. The displacements of the two Al2 atoms have the same magnitude but opposite directions, indicating a paired motion between them. As a consequence, these modes have higher frequencies than the other Al modes. The first three new features are largely related to the motions of the two H3 and the two Al2 atoms in the double-bridge structure. (4) A set of two peaks around 1050 cm<sup>-1</sup> are associated with the out-of-plane motion of four H4 atoms in the hexagonal-ring structure shown in Fig.  $1(b)$  $1(b)$ . (5) The set of high-frequency peaks around 2012 cm−1 are associated with H1 atoms which connect two Al2 atoms in opposite directions. The angle Al2- H1-Al2 is 180°. The vibrational modes of H1 are in the *ab* plane and along the Al2-H1-Al2 line. These new features displayed in the  $\gamma$ -AlH<sub>3</sub> phonon DOS can serve as indicators of these special Al and H arrangements.

Phonons at the  $\Gamma$  point can be classified according to the irreducible representations of the  $D_{3d}$  and  $D_{2h}$  point groups of  $\alpha$ -AlH<sub>3</sub> and  $\gamma$ -AlH<sub>3</sub>, respectively. The Raman and infrared frequencies are calculated at their equilibrium geometries of the experimental lattice parameters. The calculated results are listed in Table [III](#page-4-2) for  $\alpha$ -AlH<sub>3</sub> and in Table [IV](#page-6-6) for  $\gamma$ -AlH<sub>3</sub>, respectively.

### **IV. CONCLUSION**

We have performed pseudopotential density-functional calculations to study the electronic and phonon vibrational

properties for the newly reported aluminum hydride  $\gamma$ -AlH<sub>3</sub>. The calculated structural parameters are in good agreement with results from the diffraction experiments. Our energetic study for the AlH<sub>3</sub> system indicates that  $\gamma$ -AlH<sub>3</sub> is less stable than  $\alpha$ -AlH<sub>3</sub> by ~1.2 KJ/mol with the zero-point energy included. The unique double-bridge configuration in  $\gamma$ -AlH<sub>3</sub> is investigated by examining the electronic properties and phonon vibrational modes. It is found that the double-bridge arrangement modifies the binding between H and Al atoms. The projected electronic density of states indicates that interaction exists between the double-bridge H3 atoms and that the interaction between H3-*s* and higher-energy Al2-*p* and *d* states is enhanced. The latter yields a higher electronic energy in  $\gamma$ -AlH<sub>3</sub>. New features in the phonon vibrational spectrum associated with the double-bridge bonds and the hexagonal-ring complex are also identified.

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